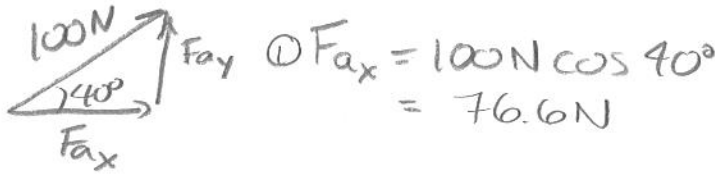


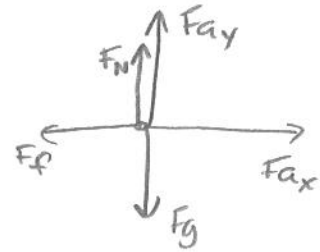
# Review for Test - Advanced Forces

## ANSWERS

1)



$$\textcircled{1} F_{ax} = 100\text{N} \cos 40^\circ = 76.6\text{N}$$

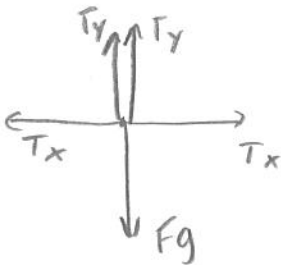


$$\textcircled{2} F_{net} = 0$$

$$F_{ax} = F_f$$

$$F_f = 76.6\text{N} \rightarrow \textcircled{B}$$

2)



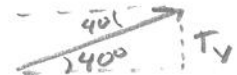
$$\textcircled{1} F_g = mg = (75\text{kg})(9.8\text{m/s}^2) = 735\text{N}$$

$$\textcircled{2} F_g = 2T_y$$

$$T_y = \frac{F_g}{2} = \frac{735\text{N}}{2}$$

$$T_y = 367.5\text{N}$$

③



$$\sin 40^\circ = \frac{T_y}{T}$$

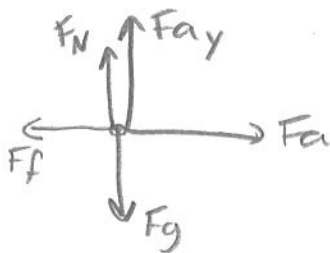
$$T = \frac{T_y}{\sin 40^\circ}$$

$$T = \frac{367.5\text{N}}{\sin 40^\circ}$$

$$T = 572\text{N}$$

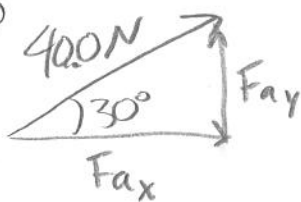
↳ ④

3)



$$F_g = mg = (6.0\text{kg})(9.8\text{m/s}^2) = 58.8\text{N}$$

①



$$F_{ax} = 40.0\text{N} \cos 30^\circ = 34.6\text{N}$$

$$F_{ay} = 40.0\text{N} \sin 30^\circ = 20.0\text{N}$$

→

3) Continued

$$\textcircled{2} F_g = F_N + F_{ay}$$

$$F_N = F_g - F_{ay}$$

$$= 58.8 \text{ N} - 20.0 \text{ N}$$

$$= 38.8 \text{ N}$$

$$\textcircled{3} F_{\text{net}} = ma$$

$$= (6.0 \text{ kg})(3.19 \text{ m/s}^2)$$

$$= 19.14 \text{ N}$$

$$\textcircled{4} F_{\text{net}} = F_{ax} - F_f$$

$$F_f = F_{ax} - F_{\text{net}}$$

$$= 34.6 \text{ N} - 19.14 \text{ N}$$

$$= 15.46 \text{ N}$$

$$\textcircled{5} F_f = \mu F_N$$

$$\mu = \frac{F_f}{F_N}$$

$$= \frac{15.46 \text{ N}}{38.8 \text{ N}}$$

$$= 0.40$$

$$\begin{aligned} 4) \quad ① \quad F_{g \text{ hang}} &= mg \\ &= (10 \text{ kg})(9.8 \text{ m/s}^2) \\ &= 98 \text{ N} \end{aligned}$$

② Find  $F_f$  (on 5 kg mass)

$$\begin{aligned} F_g &= mg \\ &= (5 \text{ kg})(9.8 \text{ m/s}^2) \\ &= 49 \text{ N} = F_N \end{aligned}$$

$$\begin{aligned} F_f &= \mu F_N \\ &= (0.5)(49 \text{ N}) \\ &= 24.5 \text{ N} \end{aligned}$$

$$\begin{aligned} ③ \quad F_{\text{net}} &= F_{g \text{ hang}} - F_f \\ &= 98 \text{ N} - 24.5 \text{ N} \\ &= 73.5 \text{ N} \end{aligned}$$

$$④ \quad F_{\text{net}} = ma$$

$$a = \frac{F_{\text{net}}}{m}$$

$$= \frac{73.5 \text{ N}}{15 \text{ kg}}$$

$$15 \text{ kg}$$

$$\boxed{a = 4.9 \text{ m/s}^2}$$

$$\begin{aligned} 5) \textcircled{1} F_{\text{net}} &= ma \\ &= (9.0 \text{ deg})(1.8 \text{ M/s}^2) \\ &= 16.2 \text{ N} \end{aligned}$$

$$\textcircled{2} F_{\text{net}} = F_{\text{ghang}} - F_f$$

$$\begin{aligned} F_{\text{ghang}} &= F_{\text{net}} + F_f \\ &= 16.2 \text{ N} + 6.3 \text{ N} \\ &= 22.5 \text{ N} \end{aligned}$$

$$\textcircled{3} F_{\text{ghang}} = mg$$

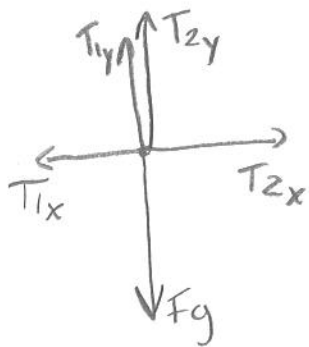
$$g = \frac{F_{\text{ghang}}}{m}$$

$$= \frac{22.5 \text{ N}}{3.0 \text{ kg}}$$

$$g = 7.5 \text{ M/s}^2$$

$$g = 7.5 \text{ M/s}^2$$

6)



$$\begin{aligned} \textcircled{1} \quad T_{1x} &= T_{2x} \\ T_1 \cos 35^\circ &= T_2 \cos 70^\circ \\ T_1 &= T_2 \frac{\cos 70^\circ}{\cos 35^\circ} \\ T_1 &= T_2 (0.418) \end{aligned}$$

$$\begin{aligned} F_g &= mg \\ &= (50 \text{ kg})(9.8 \frac{\text{m}}{\text{s}^2}) \\ &= 490 \text{ N} \end{aligned}$$

$$\textcircled{2} \quad F_g = T_{1y} + T_{2y}$$

$$490 \text{ N} = T_1 \sin 35^\circ + T_2 \sin 70^\circ$$

$$490 \text{ N} = (0.418) T_2 \sin 35^\circ + T_2 \sin 70^\circ$$

$$490 \text{ N} = 0.240 T_2 + 0.940 T_2$$

$$490 \text{ N} = 1.18 T_2$$

$$T_2 = \frac{490 \text{ N}}{1.18}$$

$$\boxed{T_2 = 415 \text{ N}}$$

$$T_1 = T_2 (0.418)$$

$$T_1 = (415 \text{ N})(0.418)$$

$$\boxed{T_1 = 173 \text{ N}}$$

$$\begin{aligned} 7) \textcircled{1} \quad F_{\text{net}} &= F_{\text{hang}} - F_f \\ &= 19.6 \text{ N} - 5.0 \text{ N} \\ &= 14.6 \text{ N} \end{aligned}$$

$$\begin{aligned} \textcircled{2} \quad F_{\text{net}} &= ma \\ a &= \frac{F_{\text{net}}}{m} \\ &= \frac{14.6 \text{ N}}{5.0 \text{ kg}} \\ &= 2.92 \frac{\text{m}}{\text{s}^2} \end{aligned}$$

$$\textcircled{3} \text{ isdate } 3.0 \text{ kg}$$

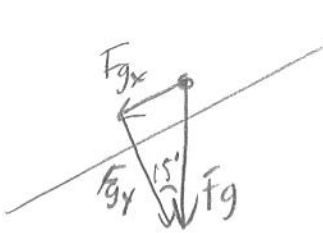
$$\begin{aligned} F_{\text{net}} &= ma \\ &= (3.0 \text{ kg})(2.92 \frac{\text{m}}{\text{s}^2}) \\ &= 8.76 \text{ N} \end{aligned}$$

$$F_{\text{net}} = T - F_f$$

$$\begin{aligned} T &= F_{\text{net}} + F_f \\ &= 8.76 \text{ N} + 5.0 \text{ N} \end{aligned}$$

$$\boxed{T = 13.76 \text{ N}}$$

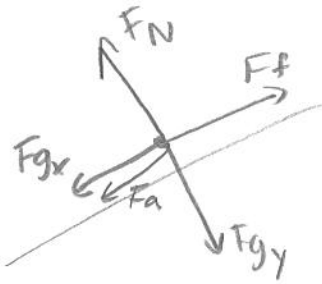
8)



$$\begin{aligned} \textcircled{1} F_g &= mg \\ &= (125 \text{ kg})(9.8 \text{ m/s}^2) \\ &= 1225 \text{ N} \end{aligned}$$

$$\begin{aligned} F_{gx} &= F_g \sin 15^\circ \\ &= 1225 \text{ N} \sin 15^\circ \\ &= 317 \text{ N} \end{aligned}$$

$$\begin{aligned} F_{gy} &= F_g \cos 15^\circ \\ &= 1225 \text{ N} \cos 15^\circ \\ &= 1183 \text{ N} \end{aligned}$$



$$\begin{aligned} \textcircled{2} F_f &= \mu F_N & F_N &= F_{gy} \\ &= (0.40)(1183 \text{ N}) & &= 1183 \text{ N} \\ &= 473 \text{ N} \end{aligned}$$

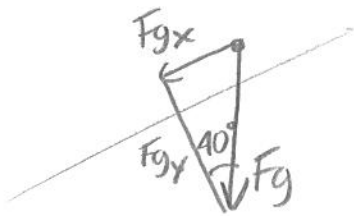
$$\begin{aligned} \textcircled{3} F_{\text{net}} &= F_{gx} + F_a - F_f \\ &= 317 \text{ N} + 250 \text{ N} - 473 \text{ N} \\ &= 94 \text{ N} \end{aligned}$$

$$\textcircled{4} F_{\text{net}} = ma$$

$$\begin{aligned} a &= \frac{F_{\text{net}}}{m} \\ &= \frac{94 \text{ N}}{125 \text{ kg}} \end{aligned}$$

$$\boxed{a = 0.75 \text{ m/s}^2}$$

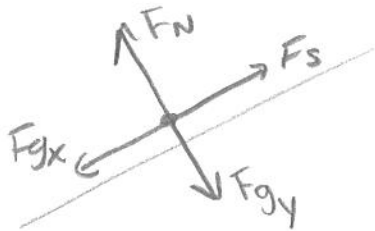
9)



$$\textcircled{1} F_g = mg = (50 \text{ kg})(9.8 \text{ m/s}^2) = 490 \text{ N}$$

$$F_{gx} = 490 \text{ N} \sin 40^\circ = 315 \text{ N}$$

$$F_{gy} = 490 \text{ N} \cos 40^\circ = 375 \text{ N}$$



$$\textcircled{2} F_{gx} = F_s \quad (\text{equilibrium})$$

$$F_s = 315 \text{ N}$$

$$F_{\text{net}} = 0$$

$$\textcircled{3} F_s = kx$$

$$x = \frac{F_s}{k}$$

$$= \frac{315 \text{ N}}{250 \text{ N/m}}$$

$$= 1.26 \text{ m}$$

$$= 1.26 \text{ m}$$

$$\boxed{x = 126 \text{ cm}}$$

$$10) F_{\text{net}} = ma$$

$$a = \frac{F_{\text{net}}}{m}$$

$$= \frac{35 \text{ N}}{10 \text{ kg}}$$

$$a = 3.5 \text{ m/s}^2$$

Isolate 5.0 kg

$$F_{\text{net}} = ma$$

$$= (5.0 \text{ kg})(3.5 \text{ m/s}^2)$$

$$= 17.5 \text{ N}$$

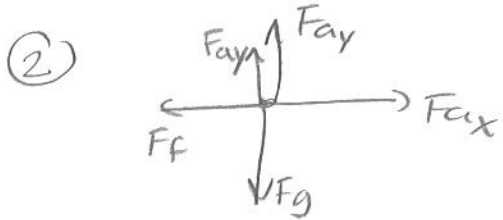
$$F_{\text{net}} = F_a - T$$

$$T = F_a - F_{\text{net}}$$

$$= 35 \text{ N} - 17.5 \text{ N}$$

$$\boxed{T = 17.5 \text{ N}}$$

$$\begin{aligned}
 \text{11) } \textcircled{1} \quad F_{\text{net}} &= ma \\
 &= (5.0 \text{ kg})(4.0 \text{ m/s}^2) \\
 &= 20 \text{ N}
 \end{aligned}$$



$$\begin{aligned}
 F_{\text{net}} &= F_{\text{ax}} - F_f \\
 F_{\text{ax}} &= F_{\text{net}} + F_f \\
 &= 20 \text{ N} + 45 \text{ N} \\
 &= 65 \text{ N}
 \end{aligned}$$

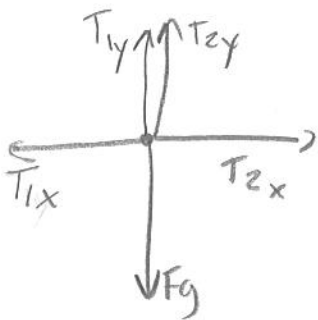
③



$$\begin{aligned}
 \cos 40^\circ &= \frac{F_{\text{ax}}}{F} \\
 F &= \frac{F_{\text{ax}}}{\cos 40^\circ} \\
 &= \frac{65 \text{ N}}{\cos 40^\circ} \\
 \boxed{F} &= \boxed{85 \text{ N}}
 \end{aligned}$$



12)



$$\begin{aligned} \textcircled{1} \quad T_{1x} &= T_{2x} \\ &= T_2 \cos 30^\circ \\ &= (15.0 \text{ N}) \cos 30^\circ \\ T_{1x} &= 12.99 \text{ N} \end{aligned}$$

$$\textcircled{2} \quad T_{1y} + T_{2y} = F_g$$

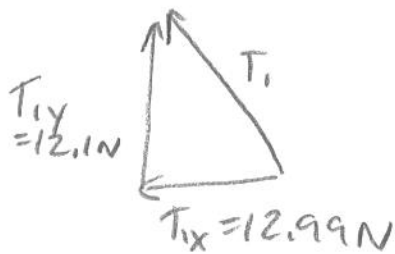
$$T_{1y} + T_2 \sin 30^\circ = (2 \text{ kg})(9.8 \text{ m/s}^2)$$

$$T_{1y} + (15.0 \text{ N}) \sin 30^\circ = 19.6 \text{ N}$$

$$T_{1y} + 7.5 \text{ N} = 19.6 \text{ N}$$

$$T_{1y} = 12.1 \text{ N}$$

③



$$\begin{aligned} T_1 &= \sqrt{T_{1x}^2 + T_{1y}^2} \\ &= \sqrt{(12.99 \text{ N})^2 + (12.1 \text{ N})^2} \end{aligned}$$

$$\boxed{T_1 = 17.8 \text{ N}}$$

13) ①  $\Delta d = 8.0 \text{ m}$   
 $a = ?$   
 $v_i = 0$   
 $\Delta t = 3.0 \text{ s}$

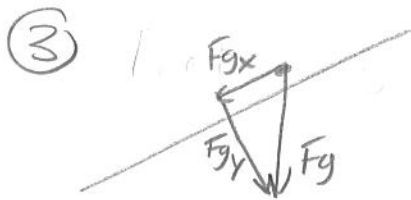
$$\Delta d = \cancel{v_i \Delta t} + \frac{1}{2} a (\Delta t)^2$$

$$a = \frac{2\Delta d}{(\Delta t)^2}$$

$$= \frac{2(8.0 \text{ m})}{(3.0 \text{ s})^2}$$

$$a = 1.78 \text{ m/s}^2$$

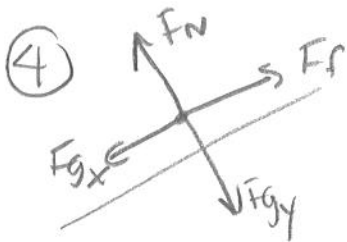
②  $F_{\text{net}} = ma$   
 $= (10.0 \text{ kg})(1.78 \text{ m/s}^2)$   
 $= 17.8 \text{ N}$



$$F_g = mg = (10.0 \text{ kg})(9.8 \text{ m/s}^2) = 98 \text{ N}$$

$$F_{gx} = 98 \text{ N} \sin 28^\circ = 46 \text{ N}$$

$$F_{gy} = 98 \text{ N} \cos 28^\circ = 86.5 \text{ N}$$



$$F_{\text{net}} = F_{gx} - F_f$$

$$F_f = F_{gx} - F_{\text{net}}$$

$$= 46 \text{ N} - 17.8 \text{ N}$$

$$= 28.2 \text{ N}$$

$$F_{gy} = F_N$$

⑤  $F_f = \mu F_N$

$$\mu = \frac{F_f}{F_N}$$

$$= \frac{28.2 \text{ N}}{86.5 \text{ N}}$$

$$= 0.33$$

$$\boxed{\mu = 0.33}$$

14) ① From graph  $g = \text{slope}$

$$= \frac{20\text{N} - 4\text{N}}{10\text{kg} - 2\text{kg}}$$

$$= \frac{16\text{N}}{8\text{kg}}$$

$$g = 2 \text{ m/s}^2$$

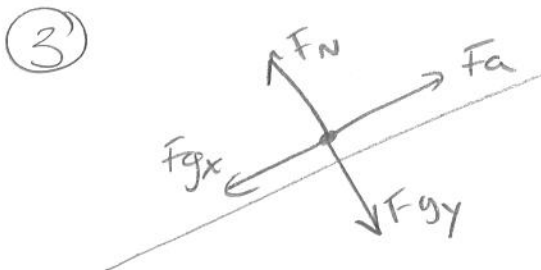
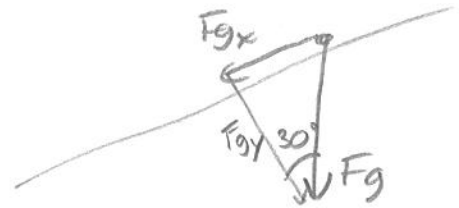
②  $F_g = mg$

$$= (80\text{kg})(2.0\text{m/s}^2)$$

$$= 160\text{N}$$

$$F_{gx} = 160\text{N} \sin 30^\circ$$

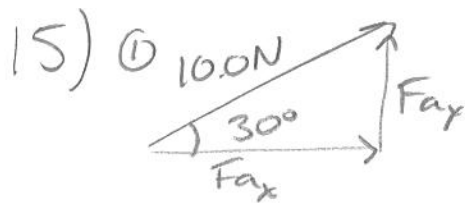
$$= 80\text{N}$$



Equilibrium (constant speed)

$$\rightarrow F_{gx} = F_a$$

$$\boxed{F_a = 80\text{N}}$$

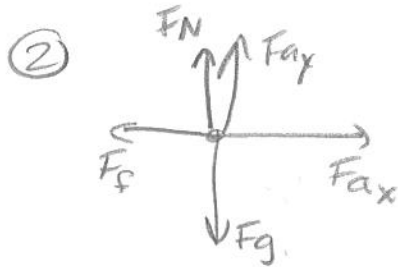


$$F_{ax} = 10.0 \text{ N} \cos 30^\circ$$

$$= 8.66 \text{ N}$$

$$F_{ay} = 10.0 \text{ N} \sin 30^\circ$$

$$= 5.0 \text{ N}$$



$$F_g = F_N + F_{ay}$$

$$F_N = F_g - F_{ay}$$

$$= 19.6 \text{ N} - 5.0 \text{ N}$$

$$F_N = 14.6 \text{ N}$$

③  $F_f = \mu F_N$

$$= (0.15)(14.6 \text{ N})$$

$$= 2.19 \text{ N}$$

④  $F_{\text{net}} = F_{ax} - F_f$

$$= 8.66 \text{ N} - 2.19 \text{ N}$$

$$F_{\text{net}} = 6.47 \text{ N}$$

⑤  $F_{\text{net}} = ma$

$$a = \frac{F_{\text{net}}}{m}$$

$$= \frac{6.47 \text{ N}}{2.0 \text{ kg}}$$

$$= 3.2 \text{ m/s}^2$$

$$\boxed{a = 3.2 \text{ m/s}^2}$$