

Answers: Practice Test (W, P, E) - 2013

1) A) B \rightarrow vertical force, horizontal displacement
C \rightarrow small Δd
D \rightarrow no friction = very small force need

2) A) KE increases then decreases
KE as a function of position is linear

$$3) F_{\text{apx}} = 2.0 \times 10^3 \text{ N} \times \cos 20^\circ \\ = 1879 \text{ N}$$

$$W = F \cdot \Delta d \\ = (1879 \text{ N})(50.0 \text{ m}) \\ = 93950 \text{ J}$$

$$P = \frac{W}{\Delta t} \\ = \frac{93950 \text{ J}}{5.0 \text{ s}} \\ = \underline{\underline{1.9 \times 10^4 \text{ W}}}$$

oops! 5) $PE_i - W_f = KE_f$
 $KE_f = mgh - F \cdot \Delta d$
 $= (1.0 \text{ kg})(9.8 \text{ m/s}^2)(0.25 \text{ m}) - (1.325 \text{ N})(0.75 \text{ m})$
 $= 1.456 \text{ J}$

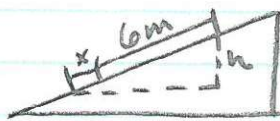
$$KE = \frac{1}{2} m v^2$$

$$v^2 = \frac{2KE}{m} \\ = \frac{2(1.456 \text{ J})}{1.0 \text{ kg}}$$

$$v^2 = 2.912 \text{ m}^2/\text{s}^2$$

$$v = \underline{\underline{1.7 \text{ m/s}}}$$

oops! 6)



$$\sin 30^\circ = \frac{h}{6m+x} \rightarrow h = \sin 30^\circ (6m+x)$$
$$h = 3m + 0.5x$$

$$E_p = E_e$$
$$mgh = \frac{1}{2} kx^2$$

$$(20\text{kg})(9.8\frac{\text{m}}{\text{s}^2})(3m + 0.5x) = \frac{1}{2} (200\text{N/m})x^2$$

$$588\text{J} + 98x = 100x^2 \quad \text{quadratic!}$$
$$0 = 100x^2 - 98x - 588\text{J}$$

$$x = \frac{98 \pm \sqrt{(98)^2 - 4(100)(-588)}}{2(100)}$$

$$x = \frac{98 \pm 495}{200} \rightarrow \boxed{x = 2.97\text{m}} \quad \text{or } x = \cancel{-1.99\text{m}}$$

oops! 4)

$$W = \Delta KE$$
$$F\Delta d = KE_f - KE_i$$
$$F\Delta d = -\frac{1}{2} m v^2$$

$$F = \frac{-1 m v^2}{2 \Delta d}$$

$$= \frac{-1 (0.275\text{kg})(25\text{m/s})^2}{2 (0.30\text{m})}$$

$$= \underline{\underline{286\text{N}}}$$

495

$$7) PE_i = KE_f$$
$$mgh = \frac{1}{2} m v^2$$

$$v^2 = 2gh$$
$$= 2(9.8\text{m/s}^2)(0.1\text{m})$$

$$v^2 = 1.96\text{m}^2/\text{s}^2$$

$$v = \underline{\underline{1.4\text{m/s}}}$$

$$\begin{aligned}
 8) \quad PE_i - W &= 0 && (\text{use } 5.0\text{m as } PE=0) \\
 PE_i &= W_f \\
 mgh &= F\Delta d \\
 F &= \frac{mgh}{\Delta d} \\
 &= \frac{(200\text{kg})(9.8\text{m/s}^2)(5.0\text{m})}{30.0\text{m}} \\
 &= \underline{\underline{327\text{N}}}
 \end{aligned}$$

$$\begin{aligned}
 9) \quad PE_i &= E_s \\
 mgh &= \frac{1}{2}kx^2 \\
 k &= \frac{2mgh}{x^2} \\
 &= \frac{2(0.75\text{kg})(0.552\text{m})}{(0.0264\text{m})^2} \\
 &= \underline{\underline{1188\text{N/m}}}
 \end{aligned}$$

$$\begin{aligned}
 10) \quad W_{\text{app}} &= PE_f \\
 F\Delta d &= mgh \\
 h &= \frac{F\Delta d}{mg} \\
 &= \frac{(73.5\text{N})(0.40\text{m})}{(0.105\text{kg})(9.8\text{m/s}^2)} \\
 &= \underline{\underline{28.6\text{m}}}
 \end{aligned}$$

↳ although the question does say "from starting position", the diagram does ask for h from the top of the apparatus.

$$\begin{aligned}
 \text{ii) } E_s - W_f &= KE_f \\
 KE_f &= E_s - W_f \\
 &= \frac{1}{2} kx^2 - F_f \Delta d \\
 &= \frac{1}{2} (50 \text{ N/m}) (0.10 \text{ m})^2 - (1.225 \text{ N}) (0.10 \text{ m}) \\
 &= 0.1275 \text{ J}
 \end{aligned}$$

note: x of spring
=
 Δd for friction

$$\begin{aligned}
 \uparrow \\
 F_f &= \mu F_N & F_N &= F_g \\
 &= 0.25 (4.9 \text{ N}) \\
 &= 1.225 \text{ N}
 \end{aligned}$$

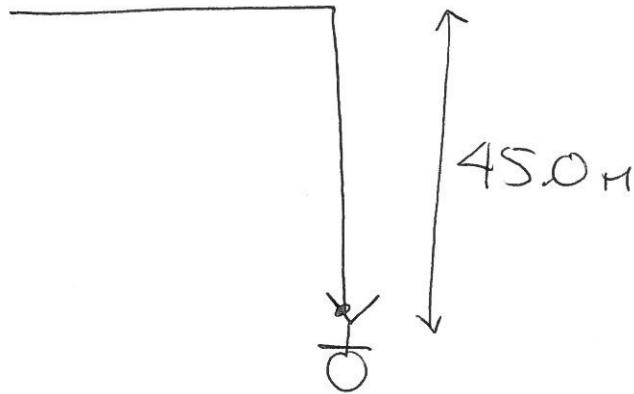
$$\begin{aligned}
 KE &= \frac{1}{2} m v^2 \\
 v^2 &= \frac{2 KE}{m} \\
 &= \frac{2 (0.1275 \text{ J})}{0.5 \text{ kg}} \\
 v^2 &= 0.51 \text{ m}^2/\text{s}^2 \\
 v &= \underline{0.71 \text{ m/s}}
 \end{aligned}$$

~~12) From bridge to max speed~~

~~$$\begin{aligned}
 PE_i &= KE_f \\
 mgh &= \frac{1}{2} m v^2 \\
 h &= \frac{v^2}{2g} \\
 &= \frac{(24.2 \text{ m/s})^2}{2(9.8 \text{ m/s}^2)} \\
 &= 29.9 \text{ m}
 \end{aligned}$$~~



#13.



$$x = 45.0 \text{ m} - 30.0 \text{ m} \\ = 15.0 \text{ m}$$

$$\textcircled{1} E_{pi} = E_{uf} + E_e$$

$$\begin{aligned} E_{uf} &= E_{pi} - E_e \\ &= mgh - \frac{1}{2} kx^2 \\ &= (62 \text{ kg})(9.8 \frac{\text{m}}{\text{s}^2})(45.0 \text{ m}) - \frac{1}{2} (175 \text{ N/m})(15.0 \text{ m})^2 \\ &= 27\,342 \text{ J} - 19\,687.5 \text{ J} \\ &= 7654.5 \text{ J} \end{aligned}$$

$$\textcircled{2} E_{uf} = \frac{1}{2} m v^2$$

$$v^2 = \frac{E_{uf}}{\frac{1}{2} m}$$

$$= \frac{7654.5 \text{ J}}{\frac{1}{2} (62 \text{ kg})}$$

$$v^2 = 246.9 \text{ m}^2/\text{s}^2$$

$$v = 15.7 \text{ m/s}$$