

Answers → More Practice → Work and Energy

$$\begin{aligned} 1) E_s &= \frac{1}{2} kx^2 \\ &= \frac{1}{2} (500 \frac{\text{N}}{\text{m}}) (0.05 \text{ m})^2 \\ &= \underline{\underline{0.625 \text{ J}}} \end{aligned}$$

$$\begin{aligned} 2) PE_i &= KE_f \\ mgh &= \frac{1}{2} mv^2 \\ h &= \frac{1}{2} \frac{v^2}{g} \\ &= \frac{1}{2} \frac{(3.0 \text{ m/s})^2}{(9.8 \text{ m/s}^2)} \\ &= \underline{\underline{0.46 \text{ m}}} \end{aligned}$$

3) ① Find a
 $a = ?$

$$\begin{aligned} v_i &= 4.0 \text{ m/s} \\ v_f &= 6.5 \text{ m/s} \\ \Delta t &= 2.0 \text{ s} \end{aligned}$$

$$v_f = v_i + a \Delta t$$

$$a = \frac{v_f - v_i}{\Delta t}$$

$$= \frac{6.5 \text{ m/s} - 4.0 \text{ m/s}}{2.0 \text{ s}}$$

$$a = 1.25 \text{ m/s}^2$$

② Find F_{net}

$$\begin{aligned} F_{\text{net}} &= ma \\ &= (0.900 \text{ kg})(1.25 \text{ m/s}^2) \\ &= 1.125 \text{ N} \end{aligned}$$

③ Find Δd

$$\Delta d = ?$$

$$\begin{aligned} v_i &= 4.0 \text{ m/s} \\ v_f &= 6.5 \text{ m/s} \\ \Delta t &= 2.0 \text{ s} \end{aligned}$$

$$\Delta d = \frac{(v_i + v_f) \Delta t}{2}$$

$$= \frac{(4.0 \text{ m/s} + 6.5 \text{ m/s})(2.0 \text{ s})}{2}$$

$$\Delta d = 10.5 \text{ m}$$



$$\begin{aligned}
 \textcircled{4} \quad W &= F \cdot \Delta d \\
 &= (1.125 \text{ N})(10.5 \text{ m}) \\
 &= \underline{\underline{11.8 \text{ J}}}
 \end{aligned}$$

$$\begin{aligned}
 4) \quad KE_i &= KE_f + E_s \\
 KE_f &= KE_i - E_s \\
 &= \frac{1}{2} m v^2 - \frac{1}{2} k x^2 \\
 &= \frac{1}{2} (2.0 \text{ kg})(6.0 \text{ m/s})^2 - \frac{1}{2} (2000 \text{ N/m})(0.15 \text{ m})^2
 \end{aligned}$$

$$KE_f = 13.5 \text{ J}$$

$$KE_f = \frac{1}{2} m v^2$$

$$v^2 = \frac{2 KE_f}{m}$$

$$= \frac{2(13.5 \text{ J})}{2.0 \text{ kg}}$$

$$v^2 = 13.5 \text{ m}^2/\text{s}^2$$

$$v = \underline{\underline{3.7 \text{ m/s}}}$$

$$5) \quad KE_i + W_{\text{ap}} = PE_f$$

$$PE_f = \frac{1}{2} m v_i^2 + F \cdot \Delta d$$

$$= \frac{1}{2} (50 \text{ kg})(5.0 \text{ m/s})^2 + (100 \text{ N})(40 \text{ m})$$

$$= 4625 \text{ J}$$

$$PE = mgh$$

$$h = \frac{PE}{mg}$$

$$= \frac{4625 \text{ J}}{(50 \text{ kg})(9.8 \text{ m/s}^2)}$$

$$h = \underline{\underline{9.4 \text{ m}}}$$

6) ① Find F_f

$$F_N = F_g \\ = 980\text{N}$$

$$F_f = \mu F_N \\ = (0.2)(980\text{N}) \\ = 196\text{N}$$

$$PE - W_f = KE_f$$

$$KE_f = mgh - F_f \Delta d \\ = (100\text{kg})(9.8 \frac{\text{m}}{\text{s}^2})(8.0\text{m}) - (196\text{N})(15\text{m}) \\ = 4900\text{J}$$

$$KE_f = \frac{1}{2} m v_f^2$$

$$v_f^2 = \frac{2KE_f}{m} \\ = \frac{2(4900\text{J})}{100\text{kg}}$$

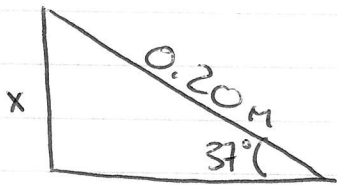
$$v_f^2 = 98 \frac{\text{m}^2}{\text{s}^2}$$

$$v_f = \underline{\underline{9.9\text{ m/s}}}$$

$$\begin{aligned}
 7) \quad W_{\text{ap}} &= PE_f \\
 &= mgh \\
 &= (50 \text{ kg})(9.8 \text{ m/s}^2)(1.7 \text{ m}) \\
 &= 833 \text{ J}
 \end{aligned}$$

$$\begin{aligned}
 W_{\text{ap}} &= F \cdot \Delta d \\
 F &= \frac{W_{\text{ap}}}{\Delta d} \\
 &= \frac{833 \text{ J}}{1.0 \text{ m}} \\
 &= \underline{\underline{833 \text{ N}}}
 \end{aligned}$$

8)



$$\begin{aligned}
 \sin 37^\circ &= \frac{x}{0.20 \text{ m}} \\
 x &= 0.20 \text{ m} \sin 37^\circ \\
 &= 0.12 \text{ m}
 \end{aligned}$$

this is how much lower the block will be.

$$\begin{aligned}
 PE_i &= E_s + KE_f \\
 KE_f &= PE_i - E_s \\
 &= mgh - \frac{1}{2} kx^2 \\
 &= (2.0 \text{ kg})(9.8 \text{ m/s}^2)(0.12 \text{ m}) - \frac{1}{2} \left(\frac{100 \text{ N}}{\text{m}} \right) (0.20)^2 \\
 &= 0.352 \text{ J}
 \end{aligned}$$

$$KE_f = \frac{1}{2} m v^2$$

$$v^2 = \frac{2(KE_f)}{m}$$

$$= \frac{2(0.352 \text{ J})}{2.0 \text{ kg}}$$

$$v^2 = 0.352 \text{ m}^2/\text{s}^2$$

$$v = \underline{\underline{0.59 \text{ m/s}}}$$